Exploring Angle Pairs



Vocabulary

Review

Use a word from the list below to complete each sentence. Use each word just once.

interior

rays

vertex

- **1.** The <u>?</u> of an *angle* is the region containing all of the points between the two sides of the angle.
- **2.** When you use three points to name an *angle*, the _? must go in the middle.
- **3.** The sides of $\angle QRS$ are ? RS and RQ.

Use the figure below for Exercises 4–7. Identify each angle as *acute*, *right*, *obtuse*, or *straight*.

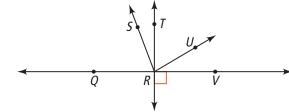
4. ∠*SRV*



5. ∠*TRS*



7. ∠*VRQ*



Vocabulary Builder

conclusion (noun) kun κιοο zhun

Other Word Forms: conclude (verb)

Definition: A **conclusion** is the end of an event or the last step in a reasoning process.

Use Your Vocabulary

Complete each sentence with conclude or conclusion.

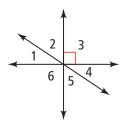
- **8.** If it rains, you can $\underline{}$? that soccer practice will be canceled.
- **9.** The last step of the proof is the _?_.

Key Concept Types of Angle Pairs

Angle Pair	Definition
Adjacent angles	Two coplanar angles with a common side, a common vertex, and no common interior points
Vertical angles	Two angles whose sides are opposite rays
Complementary angles	Two angles whose measures have a sum of 90
Supplementary angles	Two angles whose measures have a sum of 180

Draw a line from each word in Column A to the angles it describes in Column B.

Column A	Column B
10. supplementary	$\angle 1$ and $\angle 2$
11. adjacent	$\angle 2$ and $\angle 3$
12. vertical	$\angle 2$ and $\angle 5$
13. complementary	$\angle 3$ and $\angle 6$





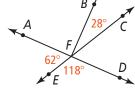
Problem 1 Identifying Angle Pairs

Got It? Use the diagram at the right. Are $\angle AFE$ and $\angle CFD$ vertical angles? Explain.

- **14.** The rays of $\angle AFE$ are \overrightarrow{FE} and $\overrightarrow{FC}/\overrightarrow{FA}$.
- **15.** The rays of $\angle CFD$ are \overrightarrow{FC} and \overrightarrow{FD} / \overrightarrow{FA} .



- **16.** \overrightarrow{FE} and are opposite rays.
- **17.** \overrightarrow{FA} and are opposite rays.
- **18.** Are $\angle AFE$ and $\angle AFE$ vertical angles?





Yes / No

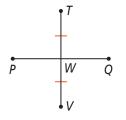
Problem 2 Making Conclusions From a Diagram

Got lt? Can you conclude that $\overline{TW} \cong \overline{WV}$ from the diagram? Explain.

19. Circle the items marked as congruent in the diagram.

$$\overline{PW}$$
 and \overline{WQ} \overline{TW} and \overline{WV} $\angle TWQ$ and $\angle PWT$ $\angle TWQ$ and $\angle VWQ$

20. Can you conclude that $\overline{TW} \cong \overline{WV}$? Why or why not?



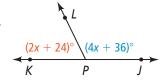
If two angles form a linear pair, then they are supplementary.

21. If $\angle A$ and $\angle B$ form a linear pair, then $m \angle A + m \angle B =$



Problem 3 Finding Missing Angle Measures

Got lt? Reasoning $\angle KPL$ and $\angle JPL$ are a linear pair, $m\angle KPL = 2x + 24$, and $m\angle JPL = 4x + 36$. How can you check that $m\angle KPL = 64$ and $m\angle JPL = 116$?



- **22.** What is one way to check solutions? Place a ✓ in the box if the response is correct. Place an ✗ in the box if it is incorrect.
 - Draw a diagram. If it looks good, the solutions are correct.
 - Substitute the solutions in the original problem statement.
- **23.** Use your answer(s) to Exercise 22 to check the solutions.

24. How does your check show that you found the correct angle measurements?



Problem 4 Using an Angle Bisector to Find Angle Measures

Got lt? \overrightarrow{KM} bisects $\angle JKL$. If $m \angle JKL = 72$, what is $m \angle JKM$?

25. Write a justification for each step.

$$m \angle JKM = m \angle MKL$$

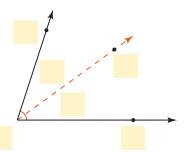
$$m \angle JKM + m \angle MKL = m \angle JKL$$

$$2m \angle JKM = m \angle JKL$$

$$m \angle JKM = \frac{1}{2}m \angle JKL$$

$$m \angle JKL =$$
, so $m \angle JKM =$.

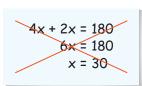
27. Now complete the diagram below.





Lesson Check • Do you UNDERSTAND?

Error Analysis Your friend calculated the value of x below. What is her error?





28. Circle the best description of the largest angle in the figure.

acute obtuse right straight

- **29.** Complete: 4x + 2x =
- **30.** What is your friend's error? Explain.

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Math Success

 $Check\ of f\ the\ vocabulary\ words\ that\ you\ understand.$

- angle complementary supplementary
 - supplementary
 - angle bisector
- vertical

Rate how well you can find missing angle measures.

