2-2

# **Conditional Statements**

## Vocabulary

#### Review

Underline the *conclusion* of each statement.

- **1.** If the weather is nice, we will go swimming.
- 2. If I ride my bike to softball practice, then I will get there on time.

#### Vocabulary Builder

converse (noun) KAHN vurs

Related Words: convert, conversion

**Definition:** The **converse** of something is its opposite.

**Word Source:** The prefix *con-*, which means "together," and *vertere*, which means "to turn," come from Latin. So, a **converse** involves changing the order of more than one thing.

#### • Use Your Vocabulary

Finish writing the converse of each statement.

3. Statement: If I study, then I pass the Geometry test.

**Converse:** If <u>?</u>, then I study.

4. Statement: If I am happy, then I laugh.

**Converse:** If <u>?</u>, then <u>?</u>.

5. Statement: If I have a summer job, then I can buy a new bicycle.

Converse: <u>?</u>.

| Rey concept Conditional Star   | ements   |          |
|--|--|----------|
| Definition   | Symbols  | Diagram  |
| A <b>conditional</b> is an <b>if</b> -then statement.  | $p \rightarrow q$  | q        |
| The <b>hypothesis</b> is the part <i>p</i> following <i>if</i> .   | Read as "If $p$ then $q$ "   |          |
| The <b>conclusion</b> is the part <i>q</i> following <i>then</i> .   | or " <mark>p</mark> implies q."  | P        |
| 5. If $p = \text{tears}$ and $q = \text{sadness}$ , what are two ways  | s to read $p \rightarrow q$ ?  |          |
|  |  |          |
|  |  |          |
|  |  |          |
| If an angle measures 130, then the angle is obtu   | ise.   |          |
| omplete each sentence with <i>if</i> or <i>then</i> .  |  |          |
| <b>7.</b> The hypothesis is the part following <u>?</u> .  |  |          |
| <b>3.</b> The conclusion is the part following <u>?</u> .  |  |          |
| 9. Circle the hypothesis. Underline the conclusion.  |  |          |
| If an angle measures 130, then the angle is obtu   | se.  |          |
|  |  |          |
| Problem 2 Writing a Conditional  |  |          |
| ot 12 How can you write "Dolphins are mamm   | als" as a conditional?   |          |
| Circle the correct statement   |  |          |
| All delphing are memmals   | ll mammals are delphins  |          |
|  | in manimals are doiphins.  |          |
| nderline the correct words to complete each state  | ment.  |          |
| nderline the correct words to complete each state  | ment.  |          |
| anderline the correct words to complete each state<br>. The set of dolphins / mammals is inside the set  | ment.<br>of dolphins / mammals .   |          |
| aderline the correct words to complete each state<br>. The set of dolphins / mammals is inside the set<br>. The smaller/larger set is the hypothesis and the | ment.<br>of <mark>dolphins / mammals</mark> .<br><mark>smaller / larger</mark> set is the cond | clusion. |

| 12.   | The   | smalle | er/larger    | set is the hypothesis and the | sm |  |  |
|---|-------|--------|--------------|-------------------------------|----|--|--|
| <b>13.</b> Use your answers to Exercises 11 and 12 to write the |       |        |              |                               |    |  |  |
|   | If _? | , then | ı <u>?</u> . |                               |    |  |  |
|   | If an | anima  | l is         |                               |    |  |  |
|   | then  | it is  |              |                               |    |  |  |

#### Problem 3 Finding the Truth Value of a Conditional

#### **Got It?** Is the conditional *true* or *false*? If it is false, find a counterexample.

If a month has 28 days, then it is February.

**14.** Cross out the month(s) that have at least 28 days.

|  | January | Februa | ary       | Marc | h       | April | May    | June     |
|--|---------|--------|-----------|------|---------|-------|--------|----------|
|  | July    | August | September |      | October | No    | vember | December |
| <b>15.</b> Is the conditional <i>true</i> or <i>false</i> ? Explain. |         |        |           |      |         |       |        |          |
|  |         |        |           |      |         |       |        |          |

| How to Write It  |   |  |  |  |  |
|--|---|--|--|--|--|
| How to write it  | Symbols   | How to Read It   |  |  |  |
| Use the given hypothesis and conclusion.                                       | $p \rightarrow q$   | If <mark>p</mark> , then <u>q</u> .  |  |  |  |
| Exchange the hypothesis and the conclusion.                                    | $q \rightarrow p$   | If <i>q</i> , then <i>p</i> .  |  |  |  |
| Negate both the <mark>hypothesis</mark> and the conclusion of the conditional. | $\sim p \rightarrow \sim q$   | If not <i>p</i> , then not <i>q</i> .  |  |  |  |
| Negate both the <mark>hypothesis</mark> and the conclusion of the converse.    | $\sim q \rightarrow \sim p$   | If not <i>q</i> , then not <i>p</i> .  |  |  |  |
| below to write each conditional.   |   |  |  |  |  |
| <b>8</b> , so $\angle A$ is obtuse.  |   |  |  |  |  |
| <u>?</u> , then <u>?</u> .   |   |  |  |  |  |
| s 98, then   | <u> </u>  |  |  |  |  |
| _, then_?  |   |  |  |  |  |
| If , then .  |   |  |  |  |  |
| <b>18.</b> Inverse If <i>not</i> _?_, then <i>not</i> _?                       |   |  |  |  |  |
| If   |   |  |  |  |  |
| then   |   |  |  |  |  |
| <b>19. Contrapositive</b> If <i>not</i> ?, then <i>not</i> ?.                  |   |  |  |  |  |
| If,  |   |  |  |  |  |
| then   |   |  |  |  |  |
|  | Exchange the hypothesis and the conclusion.<br>Negate both the hypothesis and the conclusion of the conditional.<br>Negate both the hypothesis and the conclusion of the converse.<br><b>Delow to write each conditional.</b><br>8, so $\angle A$ is obtuse.<br>? _, then ? .<br>\$98, then, then | Exchange the hypothesis and the conclusion. $q \rightarrow p$<br>Negate both the hypothesis and the conclusion<br>of the conditional. $\sim p \rightarrow \sim q$<br>Negate both the hypothesis and the conclusion<br>of the converse. $\sim q \rightarrow \sim p$<br>pelow to write each conditional.<br>8, so $\angle A$ is obtuse.<br>? _, then ? .<br>\$98, then |  |  |  |

### Problem 4 Writing and Finding Truth Values of Statements

**Got It?** What are the converse, inverse, and contrapositive of the conditional statement below? What are the truth values of each? If a statement is false, give a counterexample.

If a vegetable is a carrot, then it contains beta carotene.

- **20.** Converse: If a vegetable contains beta carotene, then <u>?</u>
- **21.** Inverse: If a vegetable is not a carrot, then <u>?</u>.
- **22.** Contrapositive: If a vegetable does not contain beta carotene, then <u>?</u>.
- **23.** The converse is true / false. The inverse is true / false. The contrapositive is true / false.
- **24.** Give counterexamples for the statements that are false.

### Lesson Check • Do you UNDERSTAND?

**Error Analysis** Your classmate rewrote the statement "You jog every Sunday" as "If you jog, then it is Sunday." What is your classmate's error? Correct it.

25. Circle the hypothesis and underline the conclusion of your classmate's conditional.

hypothesis

8

If you jog, then it is Sunday.

**Math Success** 

**conditional** 

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2

Need to

review

**26.** Circle the counterexample for your classmate's conditional.

You don't jog, and it is not Sunday.

Check off the vocabulary words that you understand.

Rate how well you can write conditional statements.

4

6

You also jog on Saturday.

conclusion

27. Write the conditional that best represents "You jog every Sunday."

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Now I

get it!