## 4-1 <br> Congruent Figures

## Vocabulary

## Review

1. Underline the correct word to complete the sentence.

A polygon is a two-dimensional figure with two / three or more segments that meet exactly at their endpoints.
2. Cross out the figure(s) that are NOT polygons.


## Vocabulary Builder

congruent (adjective) kahng Groo unt
Main Idea: Congruent figures have the same size and shape.
Related Word: congruence (noun)

## Use Your Vocabulary

3. Circle the triangles that appear to be congruent.


Write T for true or F for false.
$\qquad$ 4. Congruent angles have different measures.
$\qquad$ 5. A prism and its net are congruent figures.
6. The corresponding sides of congruent figures have the same measure.

## Key Concept Congruent Figures

Congruent polygons have congruent corresponding parts-their matching sides and angles. When you name congruent polygons, you must list corresponding vertices in the same order.
7. Use the figures at the right to complete each congruence statement.

$A B C D \cong E F G H$
$\overline{A B} \cong$
$\overline{B C} \cong$
$\overline{C D} \cong$
$\overline{D A} \cong$
$\angle A \cong$
$\angle B \cong$
$\angle C \cong$
$\angle D \cong$

## Problem 1 Using Congruent Parts

Got lt? If $\triangle W Y S \cong \triangle M K V$, what are the congruent corresponding parts?
8. Use the diagram at the right. Draw an arrow from each vertex of the first triangle to the corresponding

$$
\triangle W Y S \cong \triangle M K V
$$ vertex of the second triangle.

9. Use the diagram from Exercise 8 to complete each congruence statement.

| Sides | $\overline{W Y} \cong$ | $\overline{Y S} \cong$ | $\overline{W S} \cong$ |
| :--- | :--- | :--- | :--- |
| Angles | $\angle W \cong$ | $\angle Y \cong$ | $\angle S \cong$ |

## Problem 2 Finding Congruent Parts

Got It? Suppose that $\triangle W Y S \cong \triangle M K V$. If $m \angle W=62$ and $m \angle Y=35$, what is $m \angle V$ ? Explain.

Use the congruent triangles at the right.
10. Use the given information to label the triangles. Remember to write corresponding vertices in order.
11. Complete each congruence statement.
$\angle W \cong$

$\angle Y \cong$
$\angle S \cong$
12. Use the Triangle Angle-Sum theorem.
$m \angle S+m+m=180$, so $m \angle S=180-(+\quad+\quad$, or $\quad$.
13. Complete.

Since $\angle S \cong \quad$ and $m \angle S=\quad, m \angle V=\quad$.

## Problem 3 Finding Congruent Triangles

Got It? Is $\triangle A B D \cong \triangle C B D$ ? Justify your answer.
14. Underline the correct word to complete the sentence.

To prove two triangles congruent, show that all adjacent / corresponding parts are congruent.

15. Circle the name(s) for $\triangle A C D$.
acute
isosceles
right
scalene
16. Cross out the congruence statements that are NOT supported by the information in the figure.
$\overline{A D} \cong \overline{C D}$
$\overline{B D} \cong \overline{B D}$
$\overline{A B} \cong \overline{C B}$
$\angle A \cong \angle C$
$\angle A B D \cong \angle C B D$
$\angle A D B \cong \angle C D B$
17. You need congruence statements to prove two triangles congruent, so you
can / cannot prove that $\triangle A B D \cong \triangle C B D$.

## Theorem 4-1 Third Angles Theorem

## Theorem

If two angles of one triangle are congruent to two angles of another triangle, then the third angles are congruent.

Use $\triangle A B C$ and $\triangle D E F$ above.
18. If $m \angle A=74$, then $m \angle D=$
19. If $m \angle B=44$, then $m \angle E=$
20. If $m \angle C=62$, then $m \angle F=$
$\qquad$
If . . .

$$
\angle A \cong \angle D \text { and } \angle B \cong \angle E
$$



Then...
$\angle C \cong \angle F$ .
22. Complete the steps of the proof.

1) $\overline{A E} \cong, \overline{E B} \cong, \overline{B A} \cong$

2) Given
3) $\angle A \cong$
4) Given
5) $\angle A B E \cong$
6) Vertical angles are congruent.
7) $\angle E \cong$
8) Third Angles Theorem
9) $\triangle A E B \cong$
10) Definition of $\cong$ triangles

## Lesson Check - Do you UNDERSTAND?

If each angle in one triangle is congruent to its corresponding angle in another triangle, are the two triangles congruent? Explain.
23. Underline the correct word to complete the sentence.

To disprove a conjecture, you need one / two / many counterexample(s).
24. An equilateral triangle has three congruent sides and three $60^{\circ}$ angles. Circle the equilateral triangles below.

25. Use your answers to Exercise 24 to answer the question.

## Math Success

Check off the vocabulary words that you understand.

> congruent
polygons
Rate how well you can identify congruent polygons.


