

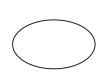
# **Congruent Figures**



# Vocabulary

#### Review

- **1.** Underline the correct word to complete the sentence.
  - A *polygon* is a two-dimensional figure with two / three or more segments that meet exactly at their endpoints.
- **2.** Cross out the figure(s) that are NOT *polygons*.











### Vocabulary Builder

congruent (adjective) kahng GROO unt

Main Idea: Congruent figures have the same size and shape.

**Related Word:** congruence (noun)

### Use Your Vocabulary

**3.** Circle the triangles that appear to be *congruent*.







Write T for true or F for false.

- **4.** Congruent angles have different measures.
- **5.** A prism and its net are *congruent* figures.
- **6.** The corresponding sides of *congruent* figures have the same measure.

#### **Key Concept** Congruent Figures

Congruent polygons have congruent corresponding parts—their matching sides and angles. When you name congruent polygons, you must list corresponding vertices in the same order.



 $ABCD \cong EFGH$ 



**7.** Use the figures at the right to complete each congruence statement.

$$\overline{AB} \cong$$

$$\overline{BC} \cong$$

$$\overline{CD} \cong$$

$$\overline{DA} \cong$$

$$\angle A \cong$$

$$\angle B \cong$$

$$\angle C \cong$$

$$\angle D \cong$$

## **Problem 1** Using Congruent Parts

**Got lt?** If  $\triangle WYS \cong \triangle MKV$ , what are the congruent corresponding parts?

8. Use the diagram at the right. Draw an arrow from each vertex of the first triangle to the corresponding vertex of the second triangle.

$$\triangle W Y S \cong \triangle M K V$$

9. Use the diagram from Exercise 8 to complete each congruence statement.

$$\overline{WY} \cong$$

$$\overline{YS}\cong$$

$$\overline{WS} \cong$$

$$\angle W \cong$$

$$\angle Y \cong$$

$$\angle S \cong$$

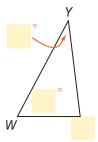


## **Problem 2** Finding Congruent Parts

**Got It?** Suppose that  $\triangle WYS \cong \triangle MKV$ . If  $m \angle W = 62$  and  $m \angle Y = 35$ , what is  $m \angle V$ ? Explain.

Use the congruent triangles at the right.

**10.** Use the given information to label the triangles. Remember to write corresponding vertices in order.





**11.** Complete each congruence statement.

$$\angle W \cong$$

$$\angle Y \cong$$

$$\angle S \cong$$



$$m \angle S + m$$

$$+ m$$

$$= 180$$
, so  $m \angle S = 180 - ( + )$ , or

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**13.** Complete.

Since 
$$\angle S \cong$$
 and  $m \angle S =$  ,  $m \angle V =$ 

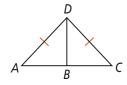
and 
$$m/S =$$

$$m \angle V =$$

#### **Got It?** Is $\triangle ABD \cong \triangle CBD$ ? Justify your answer.

**14.** Underline the correct word to complete the sentence.

To prove two triangles congruent, show that all adjacent / corresponding parts are congruent.



**15.** Circle the name(s) for  $\triangle ACD$ .

acute

isosceles

right

scalene

**16.** Cross out the congruence statements that are NOT supported by the information in the figure.

 $\overline{AD} \cong \overline{CD}$ 

 $\overline{BD} \cong \overline{BD}$ 

 $\overline{AB} \cong \overline{CB}$ 

 $\angle A \cong \angle C$ 

 $\angle ABD \cong \angle CBD$ 

 $\angle ADB \cong \angle CDB$ 

**17.** You need congruence statements to prove two triangles congruent, so you

can / cannot prove that  $\triangle ABD \cong \triangle CBD$ .

# ake note

#### **Third Angles Theorem** Theorem 4-1

#### **Theorem**

If two angles of one triangle are congruent to two angles of another triangle, then the third angles are congruent.

If . . .

 $\angle A \cong \angle D$  and  $\angle B \cong \angle E$ 





Then . . .

 $\angle C \cong \angle F$ 

#### Use $\triangle ABC$ and $\triangle DEF$ above.

**18.** If 
$$m \angle A = 74$$
, then  $m \angle D =$ 

**19.** If 
$$m \angle B = 44$$
, then  $m \angle E =$ 

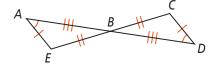
**20.** If 
$$m \angle C = 62$$
, then  $m \angle F =$ 

### **Problem 4** Proving Triangles Congruent

**Got It?** Given:  $\angle A \cong \angle D$ ,  $\overline{AE} \cong \overline{DC}$ ,

 $\overline{EB} \cong \overline{CB}, \overline{BA} \cong \overline{BD}$ 

Prove:  $\triangle AEB \cong \triangle DCB$ 



**21.** You are given four pairs of congruent parts. Circle the additional information you need to prove the triangles congruent.

A third pair of congruent sides

A second pair of congruent angles

A third pair of congruent angles

- 1) Given
- 2) Given
- 3) Vertical angles are congruent.
- 4) Third Angles Theorem
- 5) Definition of  $\cong$  triangles



# Lesson Check • Do you UNDERSTAND?

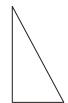
If each angle in one triangle is congruent to its corresponding angle in another triangle, are the two triangles congruent? Explain.

**23.** Underline the correct word to complete the sentence.

To disprove a conjecture, you need one / two / many counterexample(s).

**24.** An equilateral triangle has three congruent sides and three  $60^\circ$  angles. Circle the equilateral triangles below.











 $\textbf{25.} \ \ \textbf{Use your answers to Exercise 24 to answer the question.}$ 



#### **Math Success**

Check off the vocabulary words that you understand.

congruent

polygons

Rate how well you can identify congruent polygons.

Need to review



Now I