## 6-6 <br> Trapezoids and Kites

## Vocabulary

## Review

Underline the correct word to complete each sentence.

1. An isosceles triangle always has two / three congruent sides.
2. An equilateral triangle is also a(n) isosceles / right triangle.
3. Cross out the length(s) that can NOT be side lengths of an isosceles triangle.
3, 4, 5
8, 8, 10
3.6, 5, 3.6
7,11,11

## Vocabulary Builder

trapezoid (noun) trap ih zoyd
Related Words: base, leg
Definition: A trapezoid is a quadrilateral with exactly one pair of parallel sides.


Main Idea: The parallel sides of a trapezoid are called bases. The nonparallel sides are called legs. The two angles that share a base of a trapezoid are called base angles.

## Use Your Vocabulary

4. Cross out the figure that is NOT a trapezoid.

5. Circle the figure(s) than can be divided into two trapezoids. Then divide each figure that you circled into two trapezoids.


Theorem 6-19 If a quadrilateral is an isosceles trapezoid, then each pair of base angles is congruent.

Theorem 6-20 If a quadrilateral is an isosceles trapezoid, then its diagonals are congruent.
6. If $T R A P$ is an isosceles trapezoid with bases $\overline{R A}$ and $\overline{T P}$, then $\angle T \cong \angle \quad$ and $\angle R \cong \angle \quad$.
7. Use Theorem 6-19 and your answers to Exercise 6 to draw congruence marks on the trapezoid at the right.

8. If $A B C D$ is an isosceles trapezoid, then $\overline{A C} \cong$
9. If $A B C D$ is an isosceles trapezoid and $A B=5 \mathrm{~cm}$, then
$C D=$ cm .
10. Use Theorem 6-20 and your answer to Exercises 8 and 9 to label the diagram at the right.


Theorem 6-21 Trapezoid Midsegment Theorem If a quadrilateral is a trapezoid, then
(1) the midsegment is parallel to the bases, and
(2) the length of the midsegment is half the sum of the lengths of the bases.
11. If $T R A P$ is a trapezoid with midsegment $\overline{M N}$, then
(1) $\overline{M N} \|$
|
(2) $M N=\frac{1}{2}($
$+$



## Problem 2 Finding Angle Measures in Isosceles Trapezoids

Got It? A fan has 15 angles meeting at the center. What are the measures of the base angles of the congruent isosceles trapezoids in its second ring?

Use the diagram at the right for Exercises 12-16.
12. Circle the number of isosceles triangles in each wedge. Underline the number of isosceles trapezoids in each wedge.
one two three four
13. $a=360 \div=$

14. $b=\frac{180-}{2}=$
15. $c=180-\quad=$
16. $d=180-\quad=$
17. The measures of the base angles of the isosceles trapezoids are and

Got It? Algebra $\overline{M N}$ is the midsegment of trapezoid PQRS. What is $x$ ? What is MN?

18. The value of $x$ is found below. Write a reason for each step.

$$
\begin{aligned}
M N & =\frac{1}{2}(Q R+P S) \\
2 x+11 & =\frac{1}{2}[10+(8 x-12)] \\
2 x+11 & =\frac{1}{2}(8 x-2) \\
2 x+11 & =4 x-1 \\
2 x+12 & =4 x \\
12 & =2 x \\
6 & =x
\end{aligned}
$$

$\qquad$
$\qquad$
$\qquad$
$\qquad$
19. Use the value of $x$ to find $M N$.

A kite is a quadrilateral with two pairs of consecutive sides congruent and no opposite sides congruent.

## $k \in$ note

## Theorem 6-22

Theorem 6-22 If a quadrilateral is a kite, then its diagonals are perpendicular.
20. If $A B C D$ is a kite, then $\overline{A C} \perp$
21. Use Theorem 6-22 and Exercise 20 to draw congruence marks and right angle symbol(s) on the kite at the right.


## Problem 4 Finding Angle Measures in Kites

Got It? Quadrilateral $K L M N$ is a kite. What are $m \angle 1, m \angle 2$, and $m \angle 3$ ?
22. Diagonals of a kite are perpendicular, so $m \angle 1=$
23. $\triangle K N M \cong \triangle K L M$ by SSS, so $m \angle 3=m \angle N K M=$
24. $m \angle 2=m \angle 1-m \angle$
by the Triangle Exterior Angle Theorem.

25. Solve for $m \angle 2$.

## Lesson Check - Do you UNDERSTAND?

Compare and Contrast How is a kite similar to a rhombus? How is it different? Explain.
26. Place a $\checkmark$ in the box if the description fits the figure. Place an $\boldsymbol{X}$ if it does not.

| Kite | Description | Rhombus |
| :---: | :---: | :---: |
|  | Quadrilateral |  |
|  | Perpendicular diagonals |  |
|  | Each diagonal bisects a pair of opposite angles. |  |
|  | Congruent opposite sides |  |
|  | Two pairs of congruent consecutive sides |  |
|  | Two pairs of congruent opposite angles |  |
|  | Supplementary consecutive angles |  |
|  |  |  |

27. How is a kite similar to a rhombus? How is it different? Explain.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## Math Success

Check off the vocabulary words that you understand.
$\square$ trapezoidkite
baselegmidsegment

Rate how well you can use properties of trapezoids and kites.


